

Prognosis walk-through

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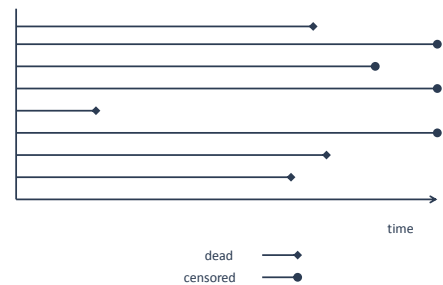
Overview

- (Brief) repetition of survival analysis
- What is a prognosis model?
- Prediction modeling vs. etiologic modeling
- How to build a prognosis model?
- Common misconceptions and errors
- Application

What is survival analysis?

- Methods to estimate the risk of death
- The time factor must be considered (somehow) since everyone dies in the end
- Typically this is done by considering the time until the occurrence of death
- Can be used for other outcomes than death

Survival data



Life table method

Year	N	# dead	Alive	Risk of death	Survival	Cumulative survival	Cumulative risk of death
1	100	8	92	$8/100=0,08$	$92/100=0,92$	0,92	0,08
2	92	7	85	$7/92=0,076$	$85/92=0,92$	$0,92 \times 0,92=0,85$	$1,0-0,85=0,15$
3	85	5	80	$5/85=0,06$	$80/85=0,95$	$0,92 \times 0,92 \times 0,95=0,80$	$1,0-0,80=0,20$

Life table with censoring

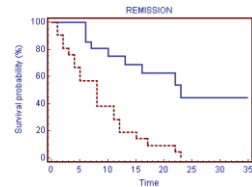
Year	N	Censored	# at risk	Dead	Alive	Risk of death	Survival	Cumulative survival	Cumulative mortality
1	100	5	97,5	8	89,5	$8/97,5=0,082$	$89,5/97,5=0,92$	0,92	$1-0,92=0,08$
2	87	4	85	7	78	$7/85=0,082$	$78/85=0,92$	$0,92 \times 0,92=0,85$	$1-0,85=0,15$
3	76	6	73	5	68	$5/73=0,068$	$68/73=0,93$	$0,85 \times 0,93=0,79$	$1-0,79=0,21$

Kaplan-Meier method

Time to event	At risk	Survival	Period specific survival	Cumulative survival
7	20	17	$17/20=0,85$	0,85
8	17	16	$16/17=0,94$	$0,85 \times 0,94 = 0,80$
10	16	15	$15/16=0,94$	$0,85 \times 0,94 \times 0,94 = 0,75$

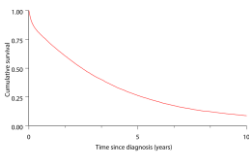
Kaplan-Meier method

- Blue line based on data from previous slide
- Survival changes at each event, but remains constant between these
- Censoring is normally not indicated in graph, but affects the size of the "jump" at the next event



Modeling survival

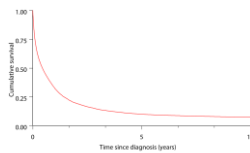
Myeloma



Median survival=2.44 years

10-year survival = 7.7%

• AML



Median survival=0.44 years

10-year survival = 7.3%

What is prognosis?

- Prognosis is a prediction of the future outcome based on the current state
- Typically deals with binary outcomes (where time is of the essence)
- Prognosis is typically dealt with using various multi-variate models

Why are we interested in prognosis?

- Patients want to know
- Doctors want to know
- Helps guide treatment allocation

How do we communicate prognosis?

"You have a 30% chance of surviving 5 years"

"Patients with your particular disease have a 30% chance of surviving 5 years"

"Patients with your particular disease, in your age group, of the same sex as you, with the same other diseases and with the same genetic mutations have a 30% chance of surviving 5 years"

...

Prognostic models

- Patients' prognosis typically depend on a range of known (and unknown) factors
- The combined effect of these factors can be measured and aggregated using multivariate statistical models
- The aim is to get a better understanding of what the prognosis is for a particular patient
- Problems with individualization of risk persists...

Prognosis vs. etiology

- Etiologic studies are typically also based on multivariate statistical models
- Importantly, for prediction/prognostication, one does not have to care (the slightest) about causality and confounding
- A prognosis model can be very accurate without inclusion of a single causal factor
- Also, absolute risks are generally preferred in prognostic studies

Prognostic models, cont.

- Depending on what you want to estimate, prognosis models are typically based on Cox regression
- The goal is to estimate what "weight" should be given to the different prognostic factors

Step-by-step development

1. Choice of possible (available) prognostic factors
 2. Collection of data
 3. Wait, wait, wait ...
 4. Design your model, choose your prognostic factors
 5. Calibrate model
 6. Validate model
 7. Test in real life – does it matter in clinical practice?
- } Focus today

Choice of predictors

- Actually quite simple!
- Depends on:
 - What data do you have access to?
 - What do you think is important, clinically?
 - How many factors do you have power to estimate?
 - What is practical to use?
 - Previous experience...

Predictors, cont.

- Typically, one includes: demographic factors, clinical parameters, laboratory tests, previous treatment*, disease characteristics
 - Current treatment not suitable
- Objective and reproducible factors
- Keep in mind that the factors must be easy to acquire for future application

Predictors, cont.

- Depending on situations, and if there is sufficient power, it can be suitable to consider interactions
- But should be based on biological/clinical reasoning, not on statistical mass-testing

Study design

- Natural choice is standard, prospective (retrospective) cohort design
- Theoretically possible to develop prognosis scores using a case-control design, but it is usually more complex

What outcome do I want to predict?

- Choice based on relevance and reproducibility
- The most robust is often all-cause mortality, but may be impractical and underpowered for most situations
- Proxy-/surrogate outcomes such as disease recurrence, disease progression or death*

Example dataset!

- Publicly available melanoma dataset on 1386 operated patients
- Available variables:
 - Time to death/recurrence, months (0-187; 0% missing)
 - Death/recurrence (0,1; 0% missing)
 - Clark's stage (1-4; 6,5% missing)
 - Sex (1,2; 0.4% missing)
 - Ulcerating tumor (0, 1; 25% missing)
 - Tumor thickness, mm (0-20 mm; 0.2% missing)
 - Localization (1-4; 0,1% missing)

Other variables

The FREQ Procedure

CLASS	Frequency	Percent	Cumulative Frequency	Cumulative Percent
1	96	6.93	96	6.93
2	77	5.57	173	12.50
3	262	18.92	435	31.42
4	423	30.52	858	61.94
4	686	49.57	1386	100.00

status	Frequency	Percent	Cumulative Frequency	Cumulative Percent
0	1862	76.62	1862	76.62
1	324	23.38	1386	100.00

sex	Frequency	Percent	Cumulative Frequency	Cumulative Percent
0	6	0.43	6	0.43
1	574	41.41	580	41.85
1	806	58.15	1386	100.00

ulcer	Frequency	Percent	Cumulative Frequency	Cumulative Percent
0	346	24.96	346	24.96
1	309	22.29	1027	72.71
1	309	22.29	1386	100.00

LECIDE	Frequency	Percent	Cumulative Frequency	Cumulative Percent
1	2	0.14	2	0.14
2	517	36.87	519	37.01
3	864	61.96	1154	82.97
4	32	2.31	1386	100.00

So, how is this done in practice?

- Commonly the cohort is based on some sort of routine data collection (e.g. through surveys or from a clinical database)
- Follow-up can be done successively or at some time-point through record linkage with a cause of death register

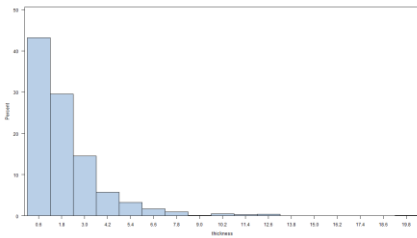
Practical details, cont.

- After the data collection, it is relevant to describe and analyze data roughly, one variable at a time:
 - Mean, median, distribution
 - Proportion missing?
 - Association with survival? Plot and consider!
 - Linear? Non-linear? Test different transformations! E.g. $1/x$, $\log(x)$, x^2 , etc.

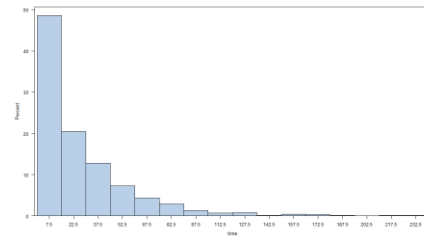
Practical details, cont.

- Some simple rule of thumb:
 - Consider the type of variable (ordinal, nominal, etc.)
 - Avoid categorization of continuous variables (unless necessary)
 - Consider truncating variables that are extremely distributed
 - Avoid including several strongly correlated variables in the same model

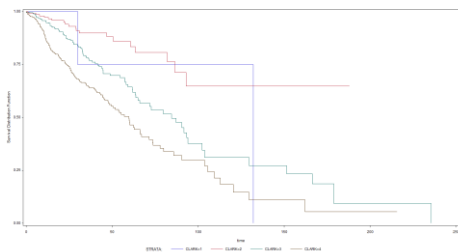
Thickness



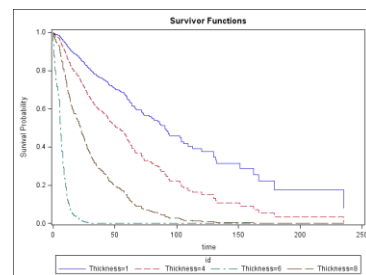
Follow-up time



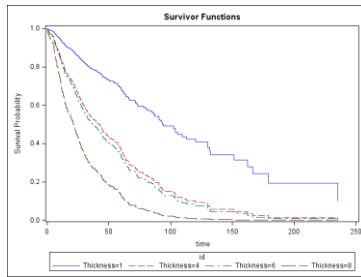
Clark (categorical)



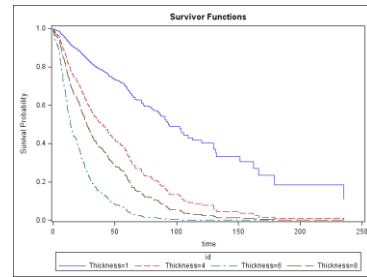
Thickness (linear function)



Thickness (linear + quadratic)



Thickness (natural spline)



Missing data

- Depending on how data is collected, some variables will always have missing values
- Why are they missing? Random? Related to outcome or prognosis? Important!
- How much is missing?
- Be cautious before excluding subjects solely based on missing data!

Missing data, forts.

- Because missing data may render an observation useless (depending on method), researchers often use some method for missing data imputation
- Imputation, in simple terms, means that one makes a qualified guess what the value should be, based on one or many other variables
- Better than throwing out the variable, but leads to loss of power and decreased predictive ability

Estimation

- Once you've picked your predictors and how they should be analyzed, the estimation is more straightforward (...), i SAS:

```
proc phreg data=melanoma;
class clark loccode;
model Time*status(0)=
thickness t2
clark
sex
ulcer
loccode
;
run;
```

Result of the first estimation

Test	Chi-Square	DF	Pr > ChiSq
Likelihood Ratio	116.6622	10	<.0001
Score	132.8765	10	<.0001
Wald	114.4569	10	<.0001

Effect	Wald		
	DF	Chi-Square	Pr > ChiSq
thickness	1	11.6622	0.0006
t2	1	0.4175	0.5182
CLARK	3	16.1900	0.0010
sex	1	3.9614	0.0466
ulcer	1	2.9613	0.0853
LOCCODE	3	2.0902	0.5539

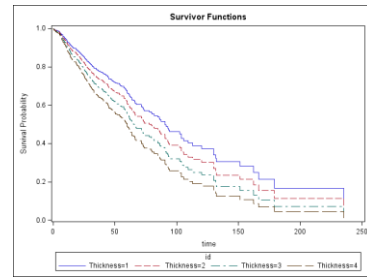
Analysis of Maximum Likelihood Estimates						
Parameter	DF	Estimate	Standard Error	Chi-Square	Pr > ChiSq	Hazard Ratio Label
thickness	1	0.181812	0.00317	11.6622	0.0006	1.201
t2	1	-0.00406	0.00628	0.4180	0.5179	0.996
CLARK	1	0.81983	0.74950	1.1985	0.2740	2.270 CLARK 1
CLARK	3	0.70234	0.25254	7.7323	0.0054	2.016 CLARK 3
CLARK	4	1.01026	0.26101	14.9815	0.0001	2.746 CLARK 4
sex	1	0.24226	0.12172	3.9614	0.0466	1.274
ulcer	1	0.24261	0.14087	2.9612	0.0853	1.274
LOCCODE	1	-0.39649	0.30958	1.6725	0.1959	0.673 LOCCODE 1
LOCCODE	2	-0.43155	0.30315	2.0265	0.1546	0.650 LOCCODE 2
LOCCODE	3	-0.43963	0.32563	1.8228	0.1770	0.644 LOCCODE 3

Result of first estimation, cont.

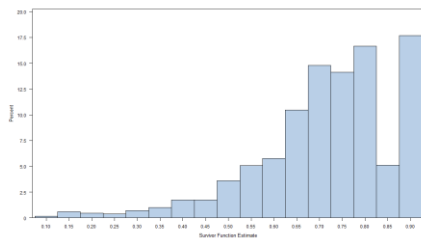
Model Fit Statistics

Criterion	Without Covariates	With Covariates
-2 Log L	3906.469	3769.827
AIC	3906.469	3809.827
SBC	3906.469	3847.635

Prediction, based on final model



Predicted 3-year survival

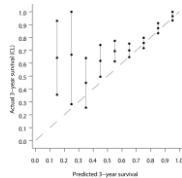


Estimation, cont.

- Techniques to reduce the number of variables are more tricky, can be forward or backwards selection
 - However, as they are based on multiple significance tests, they "consume" statistical power

Calibration (advanced)...

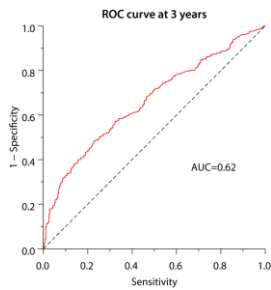
- In principle, calibration is done by comparing the model prediction with "the truth"
- The parameters are then corrected to give a more accurate prediction



Model discrimination

- Model discrimination relates to how well the model is at discriminating between those who will die and those who will not
- Traditionally, this is measured and presented as ROC-curves with AUC / c-statistic
- For survival data, where the outcome happens over time, standard methods for assessment of discriminatory ability must be estimated at a fixed time point

ROC-curve at 3-year follow-up



Validation

- The final step is validation
- This can be done both internally or externally (the latter is preferable)

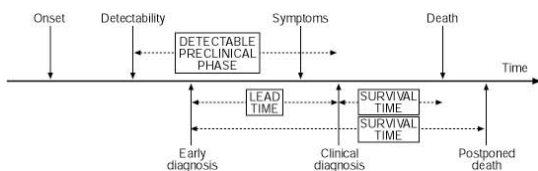
Common errors

- Power
- Systematic errors
 - External validity (due to systematic differences with other populations, e.g. due to lead time)
 - Changing treatment
- Model assumptions

Power

- Can be difficult to assess a priori
- A rule of thumb is that you need 10 patients with the outcome for each included variable – more data, however, is always better!
- More power is needed if one plans to employ variable reduction or test for interactions

Consideration of lead time



Application

- Generally difficult to apply a prognosis model without access to a computer, but examples can be found online:
http://www3.mdanderson.org/app/medcalc/index.cfm?page_name=coloncancer

Recommended reading

- Steyerberg, Clinical prediction models
- Harrell, FE *et al.* Multivariable prognostic models: ..., *Stats in medicine*, 1996
- Royston P, *et al.* Diagnosis and prognostic research..., *BMJ* 2009

